

1 Soft-wired long-term memory in a natural recurrent neuronal network

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Recurrent neuronal networks are known to be endowed with fading (short-term) memory, whereas long-term memory is usually considered to be hard-wired in the network connectivity via Hebbian learning, for instance. Here we use the neuronal network of the roundworm *C. elegans* to show that recurrent architectures in living organisms can exhibit long-term memory without relying on specific hard-wired modules. We applied a genetic algorithm, using a binary genome that encodes for inhibitory-excitatory connectivity, to solve the unconstrained optimization problem of fitting the experimentally observed dynamics of the worm's neuronal network. Our results show that the network operates in a complex chaotic regime, as measured by the permutation entropy. In that complex regime, the response of the system to repeated presentations of a time-varying stimulus reveals a consistent behavior that can be interpreted as long-term memory. This memory is soft-wired, since it does not require structural changes in the network connectivity, but relies only on the system dynamics for encoding.

14 Keywords: Feedback, excitatory-inhibitory balance, reservoir computing, consistency,
15 generalized synchronization

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16 **A common manifestation of our ability to remember the past is the consistence of our re-**
17 **sponses to repeated presentations of stimuli across time. Complex chaotic dynamics is known**
18 **to produce such reliable responses in spite of its characteristic sensitive dependence on ini-**
19 **tial conditions, via the property of generalized chaos synchronization. In neuronal networks,**
20 **complex behavior is known to result from a combination of (i) recurrent connections and (ii)**
21 **a balance between excitation and inhibition. Here we show that those features concur in the**
22 **neuronal network of a living organism, namely *C. elegans*. This enables long-term memory**
23 **to arise in an on-line manner, without having to be hard-wired in the brain.**

24 I. INTRODUCTION

25 The nervous system of metazoans is composed of recurrent networks of neurons that allow
26 them to respond to complex stimuli, both internal and external to the organism¹⁻⁴. Such recurrent
27 architectures have inspired the design of specialized artificial neural networks^{5,6} that have revolu-
28 tionized the field of machine learning, such as those based on long short-term memory (LSTM)
29 circuits⁷⁻⁹. These systems rely on complex, hard-wired modules that provide them with memory
30 capabilities, but which are too elaborate to have emerged naturally in living brains.

31 It thus seems reasonable to ask how the memory capabilities of living neuronal networks are
32 implemented, and whether they require specific, hard-wired modules. The recurrent character
33 of biological circuits plays an important role here. While the *architecture* of recurrent neural
34 networks endows them with the capacity to store static information¹⁰, their *dynamics* provides
35 them with fading memory¹¹ and with the ability to process time-dependent information in the short
36 term, via a paradigm known as reservoir computing¹²⁻¹⁴. This capability is not hard-wired into
37 the system, but arises from the self-sustained dynamics provided by its recurrent connections: any
38 external impulse perturbation will reverberate within the network for a while, mixing nonlinearly
39 with its intrinsic dynamics¹⁵. This allows the on-line encoding of complex time-dependent inputs,
40 which can be then decoded by a dedicated readout layer, located downstream of the recurrent core
41 of the network (known as the reservoir)¹⁶. The only connections whose weights need to be trained
42 are those linking the reservoir with the readout layer, which underpins the effectiveness of this
43 information-processing paradigm¹⁷.

44 The standard reservoir computing (RC) architecture has not been widely adapted by the

45 machine-learning community, nonetheless, because more sophisticated versions of it (such as
46 the LSTM layout mentioned above) have proven more efficient with a bearable (for software-
47 engineering standards) increase in complexity. The simplicity of the basic RC structure, however,
48 makes it still an attractive candidate for complex information processing in living organisms.
49 Here we use the soil nematode *Caenorhabditis elegans* as model system, due to our complete
50 knowledge of its connectome¹⁸, to show that the architecture of living neuronal networks is com-
51 patible with the RC paradigm, and thereby displays fading (short-term) memory capabilities. To
52 our knowledge, no previous studies have examined the neuronal network of *C. elegans* from the
53 perspective of reservoir computing. Furthermore, while the existence of short-term memory in
54 recurrent neuronal networks is well documented, long-term memory is usually associated with
55 structural changes in the connection strength between neurons brought about by mechanism such
56 as Hebbian learning¹⁹. Here we show that generalized synchronization²⁰, enabled by the self-
57 sustained chaotic dynamics exhibited by recurrent networks, leads to a form of long-term memory
58 by which the system responds in the same manner to the same complex input every time. In
59 that way, our results show that long-term memory can be exhibited by natural neuronal networks
60 without specific, hard-wired memory modules.

61 **II. TOPOLOGY OF THE *C. ELEGANS* NEURONAL NETWORK**

62 The architecture of the brains of higher animals is highly intricate^{21,22} and variable²³. We
63 thus chose a simpler organism for our study, namely the above-mentioned roundworm *C. elegans*,
64 whose neural system (in fact its entire cell lineage) is small and highly consistent from individual
65 to individual. Additionally, and importantly for our purpose, the *C. elegans* connectome has been
66 fully mapped¹⁸. From the approximately 1000 somatic cells forming the hermaphrodite worm,
67 302 compose its nervous system. Those cells communicate to each other through around 6400
68 chemical synapses, 900 gap junctions and 1500 neuromuscular junctions¹⁸.

69 We used a recently published, updated connectivity map of *C. elegans*²⁴. The data source
70 provided the links between neurons and the associated weights (connection strengths, but not its
71 excitatory or inhibitory character), including not only canonical neurons, but also innervations
72 from the neural system to muscles. The dataset contained information of both electrical and
73 chemical synapses, but here we focused only on the latter, which are considered more relevant
74 for information-processing purposes. The resulting graph contained two distinct components con-

75 nected by only one link. The smaller component contained only pharyngeal neurons, according
76 to the WormAtlas database²⁵. Given that the function of those neurons is very specific, we con-
77 centrated here on the largest component, which is shown in Fig. 1a. The nodes in the figure are
78 colored according to the cell type (including muscle cells receiving innervations from neurons),
79 and the links are colored according to the type of the receiving cell.

80 The next step was to identify the recurrent core of the network. To do so, we pruned the
81 graph²⁶ by iteratively removing nodes with either no outward connections (i.e. nodes that do not
82 affect other nodes) or no inward connections (i.e. nodes that are not affected by other nodes).
83 The neurons preserved after this iterative procedure strictly belong to the reservoir, since any
84 information they send out reaches back to them eventually. The removed nodes, on the other hand,
85 fall into two classes. Those upstream of the recurrent core form the input layer (cf the two sensory
86 neurons at the left of Fig. 1a). In turn, nodes downstream of the reservoir form the readout layer
87 (cell clusters at the right of Fig. 1a). As expected, all non-neuronal cells in the network (those
88 receiving innervations) belong to the readout layer.

89 Network pruning thus shows that the *C. elegans* neuronal network displays the three network
90 components (input layer, recurrent reservoir, and readout layer) characteristic of a standard reser-
91 voir computing topology^{16,17}, as shown in Fig. 1a. We now turn to analyzing the dynamics exhib-
92 ited by this network.

93 **III. NETWORK DYNAMICS**

94 Advances in *in vivo* calcium imaging have recently allowed monitoring the dynamical activity
95 of tens of neurons in free-moving *C. elegans* worms under controlled thermosensory conditions²⁷.
96 We aimed to use such data to constrain the dynamics of the network established in Sec. II above.
97 Nine of the monitored neurons could be identified with cells listed in the connectome database
98 analyzed above²⁴. The dynamics of those neurons, measured in terms of the time-resolved calcium
99 signal in each cell, is shown in Fig. 1b. The neurons exhibited irregular waveforms, a dynamical
100 trait that is known to result from a balance between excitation and inhibition²⁸. Unfortunately
101 we could not corroborate this fact with the connectome data used in the previous section²⁴, since
102 the database contained no systematic information on the excitatory/inhibitory character of the
103 connections. This issue, together with our inability to identify most of the neurons of which
104 we had calcium signaling data, made us pursue a parameter inference approach using a genetic

105 algorithm on a dynamical model of the neuronal network.

106 To simulate the dynamics of our network, we used a standard discrete-time model in which the
107 activity of the each neuron i depends in a sigmoidal (threshold-like) manner on the inputs coming
108 from other neurons:

$$x_{i,t+1} = \tanh \left(\sum_j \omega_{ij} x_{j,t} \right) \quad (1)$$

109 where $x_{i,t}$ is the state of neuron i at time t and ω_{ij} represents the strength of the connection from
110 neuron j to neuron i , normalized such that the maximum connection strength in the network is 1.
111 The parameters ω_{ij} are positive for excitatory connections and negative for inhibitory ones.

112 Since the calcium monitoring experiments were performed under conditions of oscillat-
113 ing temperature, and two of the nine labeled neurons (AFDL and AFDR) are associated with
114 thermotaxis²⁹, we considered the experimentally measured activities of those two neurons (nor-
115 malized between +1 and -1) as inputs to the network model (ignoring incoming connections
116 acting upon them). The activity of all other neurons is computed according to model (1). The
117 fitness of the $\{\omega_{ij}\}$ parameter set is then evaluated as the mean Pearson correlation coefficient
118 between the experimental and modeled time traces of all seven remaining neurons in Fig. 1b.

119 To maximize the fitness of our network model, the genetic algorithm (Fig. 2a) begins by choos-
120 ing random signs for the connection strengths between all neurons in the network (selecting a
121 uniformly distributed random number of neurons from the network and making them inhibitory,
122 with the rest being excitatory), while their magnitudes are fixed by the values given in the database.
123 A population of 100 networks built in this manner is modeled as described above. After the dy-
125 namics is generated using Eq. (1), we evaluate the fitness for each individual network. Next, the
126 30 individuals with highest fitness were selected and used to generate an offspring of 50 children
127 by recombining the adjacency matrices of randomly generated pairs of such individuals. Recom-
128 bination was performed by selecting a cutoff neuron randomly, splitting the rows of the adjacency
129 matrix at that neuron, and the rows above it from one parent and below it from the other. This re-
130 sults in a population of 80 individuals (pooling the 30 parents and the 50 children). The remaining
131 20 individuals were replaced using mutation and immigration. Mutation consisted in selecting the
132 best individual network and changing the signs of 5 connections chosen at random. We repeated
133 this process until having 10 different mutant individuals. The last 10 individuals were introducing
134 through immigration. These individuals were created with a random distribution of excitation and
135 inhibition, as in the initial individuals of the algorithm described above (to avoid biasing the pro-

136 cess). The full set of new 100 individuals obtained is then used to start a new iteration cycle. The
137 dynamics of the optimal model resulting from the procedure described above is shown in Fig. 2b,
138 where it is compared with the experimental observations. Figure 2c shows the evolution of the
139 model with highest fitness as the genetic algorithm was iterated.

140 In order to explore systematically the fitness landscape of our network model, we run the ge-
141 netic algorithm described above for 100 iterations and 1000 realizations, starting from a corre-
142 sponding number of adjacency matrices with a random balance between excitation and inhibition
143 as described above, and identified the optimal network at each iteration, resulting in a total amount
144 of $\sim 10^5$ individuals. We then computed the fitness of the optimal individuals in each case, as
145 a function of the percentage of inhibition. The corresponding density distribution is shown in
146 Fig. 3a, and indicates that the majority of optimal individuals are also those with highest fitness,
147 and have an inhibition percentage in the range of 38% to 55%, approximately. While no quan-
148 tification of this percentage exists, to our knowledge, in the neuronal network of *C. elegans*, the
149 existence of a balanced degree of inhibition and excitation is consistent with what is usually found
150 in the brains of higher animals^{30,31}, and is also in line with the complex dynamics reported above²⁸.

151 We also quantified the degree of complexity of the dynamical behavior using a standard mea-
152 sure of complexity, namely the permutation entropy³²⁻³⁴. To that end, we extracted all 3-element
153 ordinal patterns from the time series (i.e. the triplets 012, 021, 102, etc, defined by the relative
154 order of the three elements of the triplet) and compute their frequencies p_i in the series. The per-
155 mutation entropy of order 3 is then calculated as $H = -\sum p_i \log p_i$, where the sum runs over all 3!
156 patterns and the logarithm is base 2. We performed this calculation for 8000 individuals at each
157 inhibition percentage, computing the average and standard deviation of the entropy as a function
158 of the inhibition level. The complexity of the dynamics is quantified as the average divided by
159 its standard deviation. The dependence of the resulting complexity coefficient on the inhibition
160 percentage is shown in Fig. 3b. The result confirms that the complexity of the dynamics is high
161 when the network model optimally represents the experimental observations.

162 IV. RESPONSE OF THE NETWORK TO A PULSE-TRAIN STIMULATION

163 The recurrent architecture of the *C. elegans* neuronal network revealed in Sec. II endows the
164 system with short-term memory. We conjectured that the complex dynamics shown in the previous
165 section, on the other hand, makes it possible for the network to exhibit long-term memory as well.

166 To test this hypothesis, we first examine the response to external stimulation of the optimal network
 167 identified in the previous section. This can be modeled in our neuronal network by modifying the
 168 update rule (1) as follows:

$$x_{i,t+1} = \tanh \left(v_i z_t + \sum_j \omega_{ij} x_{j,t} \right) \quad (2)$$

169 Here z_t is the external input at time t and v_i is the weight between the input and neuron i . In this
 170 model, the transfer function (hyperbolic tangent) integrates the state of the neurons in each time
 171 step with the external input that they receive. We chose the weights v_i randomly for each neuron,
 172 so that the input affects more strongly some neurons than others. The initial condition is chosen
 173 randomly for each neuron, uniformly distributed between -1 and 1 .

174 The typical response of the network to a train of square pulses alternating between two values
 175 (considered binary from simplicity, 0 or 1) is shown in Fig. 4. The duration of the 0 state is chosen
 176 constant and equal to 10 time steps, whereas that of the 1 state is randomly chosen uniformly in
 177 the interval 8 ± 2 time units. The top plot in Fig. 4a shows the input, and the bottom plot in that
 178 panel displays the dynamics of a given neuron of the network (taken to be neuron 12, ASER, in
 179 what follows). In turn, Fig. 4b shows the dynamics of all the neurons in the network, represented
 180 in grayscale from -1 to 1 . The figure shows that the stimulation leads to a continuous irregular
 181 dynamics, with each change in the input (from 0 to 1 and vice versa) eliciting a relaxational
 182 dynamics that does not repeat from pulse to pulse.

183 V. RESPONSE TO REPEATED STIMULATIONS

184 When next applied repeated presentations of the same irregular pulsed stimulus, with the goal
 185 of establishing whether the response of the network is consistent between trials. We interpret a
 186 consistent response in terms of long-term memory. As a reference, we compared the response
 187 of the network to the multiple trials with the response to subsequent pulses along time (Fig. 5a).
 188 Specifically, we applied 20 consecutive pulses to the network, focusing on its response to the drop
 189 from 1 to 0. For each of the 20 inputs, we compared all pairs of responses across 100 (identical)
 190 trials (inter-series comparison, orange intervals in Fig. 5a). We also compared the response of
 191 the network between all pairs of 20 events in the same trial along time (intra-series comparison,
 192 blue intervals in Fig. 5a), for a number of trials (526) such that in both cases the number of
 193 pairs was similar, $\sim 10^5$. Quantifying the similarity between the response pairs in terms of the
 194 Pearson correlation coefficient (Fig. 5b), we found significant differences ($p < 0.0005$ in a chi-

195 square test of homogeneity, see analysis in <https://github.com/sgalella-macasal-repo/SoftWired->
196 [Celegans](#)) between the distributions of these coefficients in the two cases, with the inter-series
197 correlation approaching 1 more frequently than the intra-series one. Thus, the network responds
198 more consistently to repeated presentations of the stimulus (change in the input from 1 to 0) across
199 trials than across time.

200 To quantify systematically this reliability, we developed a quantifier based on the cumulative
201 correlation distributions shown in Fig. 6a (obtained directly from Fig. 5b). A reliable response is
202 reflected in a later increase towards 1 in the cumulative distribution for the inter-series correlation
203 coefficients. Thus the fact that the cumulative distribution increases significantly earlier for the
204 intra-series (blue) than for the inter-series (orange) responses is an indication of the consistent be-
205 havior of the system. Such difference can be quantified systematically with the receiver-operating
206 curve (ROC) shown in Fig. 6b. The area between that curve and the 45-degree line is a good
207 estimator of the degree of reliability of the network: for equal responses across trials and across
208 time (no reliability), the two cumulative distributions would be identical and the area would be
209 zero; for perfect reliability, on the other hand, the area would be that of the full triangle above the
210 45-degree line ($1/2$). We thus define the degree of reliability R as the value of that area divided by
211 its maximum value. In the particular case of neuron 218 (Fig. 6b), that quantity is ~ 0.34 .

212 Figure 6c shows the distribution of R values for all neurons in the network, for three cases: the
213 optimal network identified with the fitting above (top panel), and two control cases corresponding
214 to excessive inhibition (middle panel) and excessive excitation (bottom panel). The figure shows
215 that in the case of the optimal fit to the experimental data (balanced excitation and inhibition) re-
216 liability is largest, being close to zero for 95% inhibition, and broad and mostly negative for 5%
217 inhibition (a negative value of R corresponds to a mostly periodic –and thus non-complex– dynam-
218 ics, which can be expected to be elicited in the network when excitation dominates). Averaging R
219 over all neurons in the network for 1000 realizations of the stimulus (and initial conditions) leads
220 to the distributions shown in Fig. 6d, which evidence the reproducibility of the results and the
221 difference in reliability between the three types of network.

222 VI. DISCUSSION

223 In this paper we have analyzed the architecture of the neuronal network of the roundworm *C.*
224 *elegans*, which has been fully mapped experimentally^{18,24,25}, and can thus be considered a real-

225 istic model system to study information processing in the brain. Our analysis of the published
226 connectome of this organism (Sec. II) reveals that a large fraction of the connections in the neu-
227 ronal system of *C. elegans* form cycles, and are therefore involved in internal feedback loops. This
228 has allowed us to establish that the topology of the *C. elegans* neuronal network is consistent with
229 the paradigm of reservoir computing (Fig. 1), in which a recurrent core of neurons encodes the
230 information arriving to it from an upstream input layer. In turn, the state of the recurrent reservoir
231 can be decoded by a downstream readout layer, provided the strengths of the connections between
232 the reservoir and the readout layer are trained properly.

233 We next implemented a genetic algorithm to fit the *in silico* behavior of the *C. elegans* neuronal
234 network to the experimentally measured dynamics of a subset of neurons (Sec. III). Our analysis
235 revealed (Fig. 2) an approximately balanced degree of excitation (positive connections) and inhi-
236 bition (negative connections). The best fit also corresponds to a maximal degree of complexity
237 of the balanced network dynamics. Both these features are shown in Fig. 3. The concurrence
238 of these two characteristics (excitation-inhibition balance and complex dynamics) is in agreement
239 with previous studies showing that neuronal networks with balanced excitation and inhibition are
240 characterized by self-sustained chaotic dynamics²⁸. Notably, chaotic systems have been reported
241 to respond consistently to complex external signals: upon repeated presentation of these signals, a
242 chaotic system is able to respond always in the same manner, in spite of the well known sensitive
243 dependence on initial conditions that characterizes chaos. This type of behavior was originally
244 termed “generalized synchronization”^{20,35,36}, and has since been reported in a variety of physical
245 systems including mechanical oscillators³⁷, lasers^{38,39}, and spatial light modulators⁴⁰.

246 The excitation-inhibition balance of the *C. elegans* neuronal network obtained from our fit to the
247 experimental data, and the subsequent complex dynamics resulting from it, makes us expect that
248 the system should respond consistently to complex inputs. In agreement with the above-mentioned
249 studies on generic chaotic systems, our results indicate that the network can indeed respond con-
250 sistently to repeated presentations of the same complex (irregular) sequence of events, even though
251 the individual responses to single events across the sequence are highly variable. In other words,
252 complex series of stimuli trigger the same dynamical trajectory in the high-dimensional phase
253 space of the neuronal network, when the stimulus is presented repeatedly in time. This behav-
254 ior builds upon the ability of the brain to encode information in its transient dynamics⁴¹. Since
255 remembering something in the long-term implies recognizing a potentially complex input by re-
256 sponding to it in the same way every time, we interpret the reliability reported here as a form of

257 a long-term memory that is encoded in the dynamics of the neuronal network, and can thus be
258 considered soft-wired rather than hard-wired in the brain.

259 The dynamics of our experimentally constrained neuronal network was generated using a
260 model widely employed in studies of artificial neural networks. This model captures the main
261 information-processing features of more detailed biophysical models such as the integrate-and-
262 fire⁴² and Hodgkin-Huxley⁴³ models, and thus we expect the same behavior to be reproduced by
263 those models. A second limitation of our study is the choice of external input considered (a binary
264 input, with the random duration of one of the two states as the only source of irregularity). This
265 choice was dictated by our need to quantify the consistency of the system response with respect
266 to a reference situation (taken here to be the response to sequential input changes comparable to
267 those being compared across trials). It would be worthwhile to explore the response of the network
268 to more complex inputs. In any case, we believe that our study points to information-processing
269 capabilities of biological networks that go beyond the paradigms considered so far.

270 ACKNOWLEDGMENTS

271 We thank Vivek Venkatachalam for kindly providing us with the experimental measurements of
272 neuronal activity in moving *C. elegans* worms. We also thank two anonymous reviewers for their
273 helpful suggestions. This work was supported by the Spanish Ministry of Science, Innovation
274 and Universities and FEDER (projects FIS2017-92551-EXP and PGC2018-101251-B-I00, and
275 “Maria de Maeztu” Programme for Units of Excellence in R&D, grant CEX2018-000792-M), and
276 by the Generalitat de Catalunya (ICREA Academia programme). M.A.C. is currently supported
277 by the EU Marie Skłodowska-Curie Training Network “NeuTouch” (contract 813713, call H2020-
278 MSCA-ITN-2018).

279 DATA AVAILABILITY STATEMENT

280 The data that support the findings of this study are available from the corresponding au-
281 thor upon reasonable request. All code used in the analysis is publicly available in GitHub
282 (<https://github.com/sgalella-macasal-repo/SoftWired-Celegans>).

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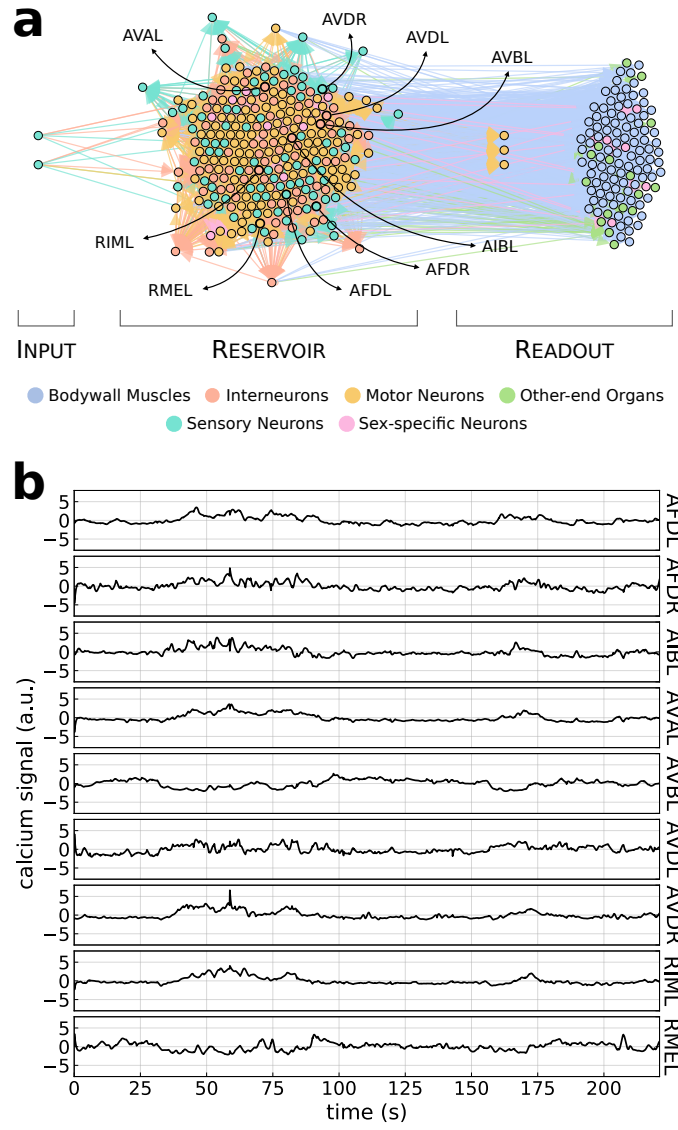


FIG. 1. **Topology and dynamics of the neuronal network of *C. elegans*.** (a) Cells listed in the connectome database of the worm²⁴ are represented as circles, colored according to the cell type (see legend), and connected by arrows indicating the presence of chemical coupling between them. The cells are clustered in such a way that the upstream input layer is located at the left of the plot (two sensory neurons on the far left), the downstream readout layer appears in the right, and the recurrent core is shown in the middle. (b) Experimentally observed calcium signal denoting the dynamical activity of nine of the neurons of the reservoir, whose identities are highlighted in panel (a).

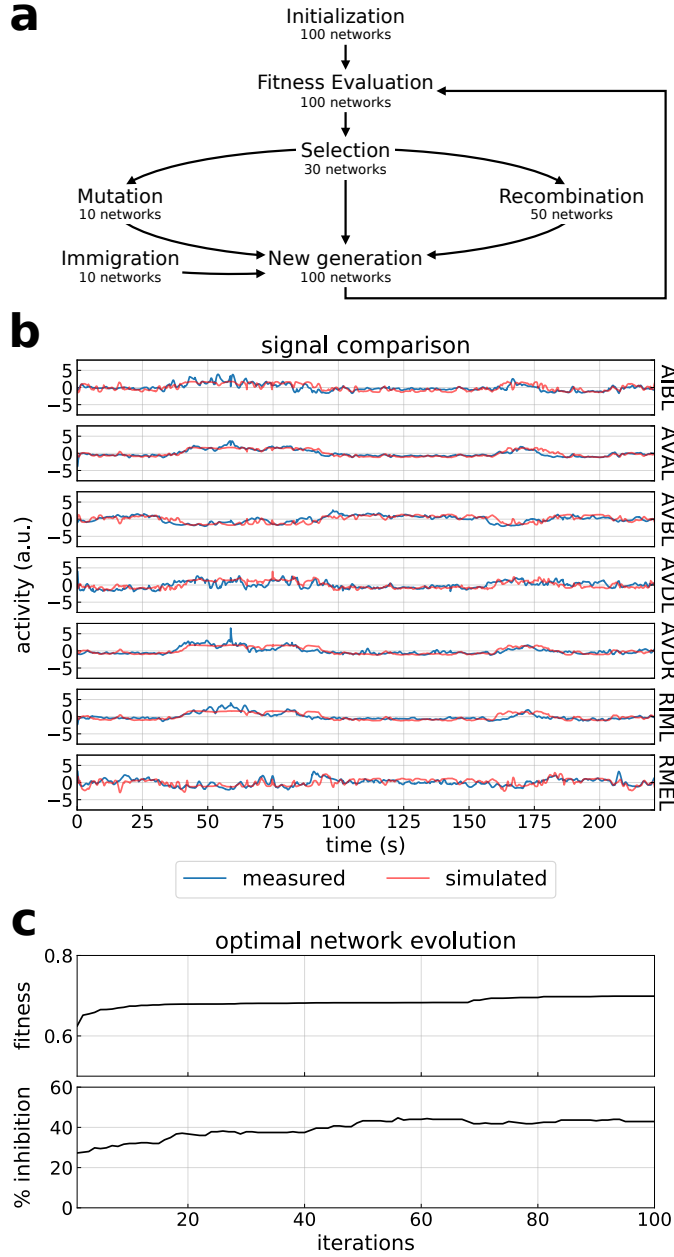


FIG. 2. Statistical inference of the connection types. (a) Scheme of the genetic algorithm used. (b) Dynamics of the seven non-input neurons generated by a particular instance of the model (blue lines) compared with the experimental data (red lines). (c) Evolution of the fitness of the optimal individual network at each iteration of the genetic algorithm (top), and corresponding percentage of inhibitory connections (bottom).

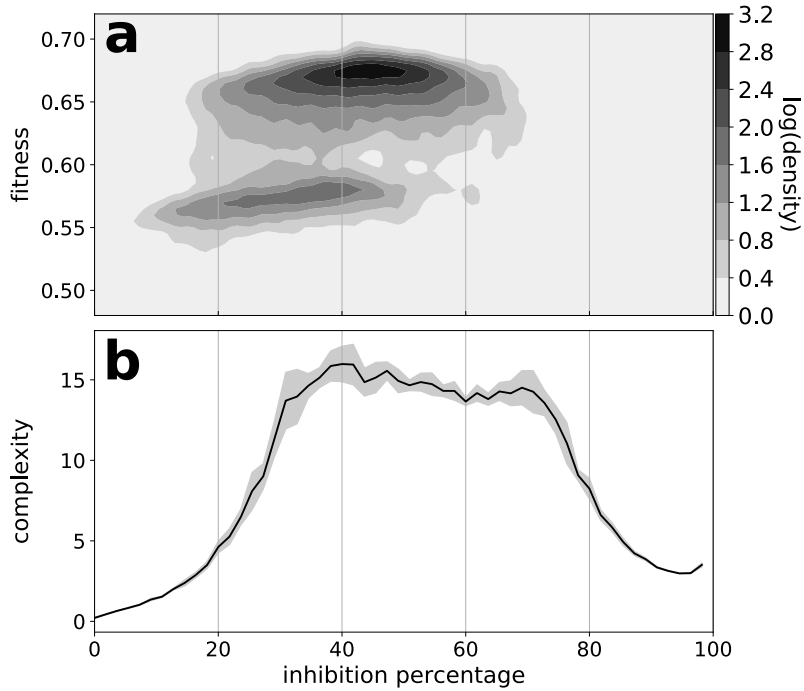


FIG. 3. Fitting to experiments reveals excitation-inhibition balance and complex dynamics. (a) Density plot of the fitness versus inhibition percentage, computed at each of 100 iterations for 1000 realizations of the genetic algorithm described in Fig. 2. The density was smoothed out with a Gaussian filter. Black corresponds to the highest density of optimal individuals. (b) Complexity of the dynamics of the network for each inhibition percentage. The black line represents the average of the permutation entropy divided by its standard deviation, calculated over 8000 realizations for each inhibition level. The grey shadowed area denotes the 95% confidence interval of this quantity, when dividing the data in 10 groups of 800 realizations per inhibition level.

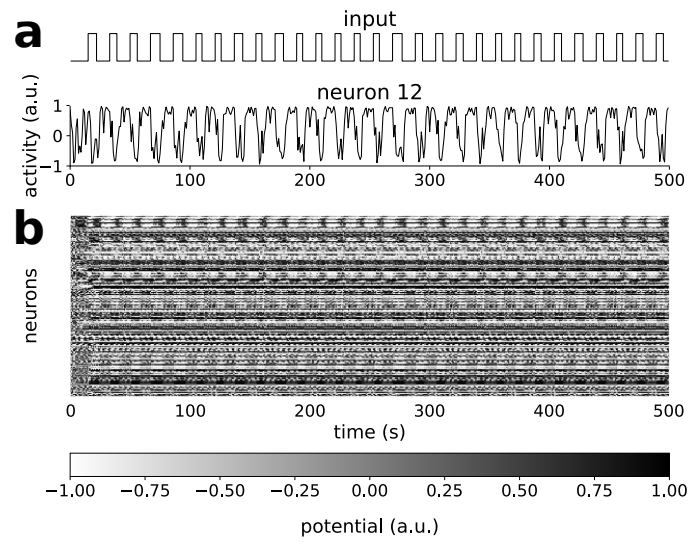


FIG. 4. Response of the optimal *C. elegans* network to pulsatile stimulation. (a) The top panel shows the input applied to the network, while the bottom panel represents the response of one of the neurons (neuron 12, ASER). (b) Response of the entire network to the input signal shown at the top of panel (a), with the state of each neuron represented in gray according with the scale bar at the bottom.

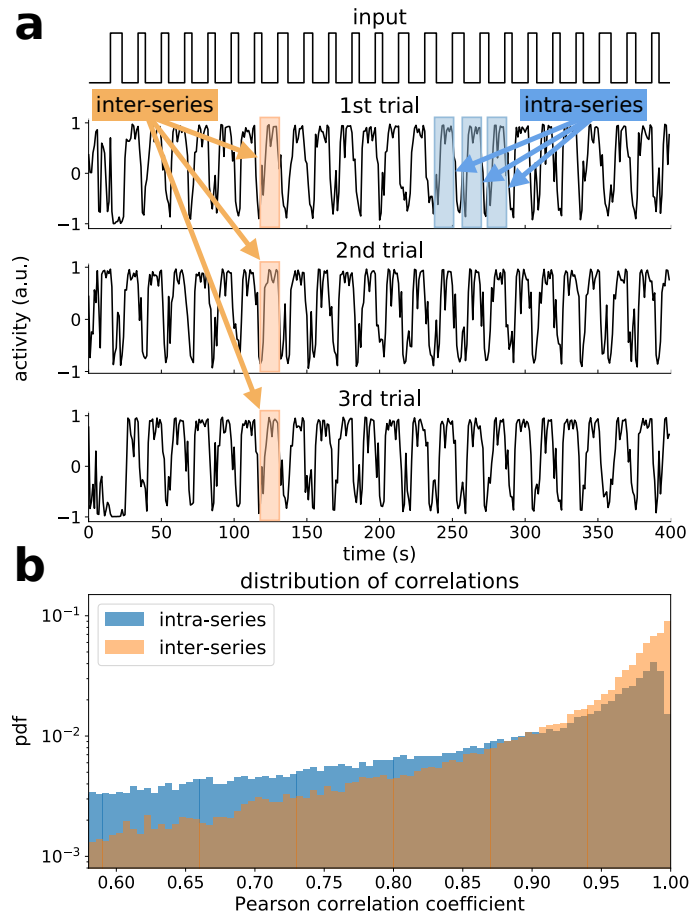


FIG. 5. Response of the optimal *C. elegans* network to repeated irregular stimulation. (a) Response of neuron 12 (bottom three panels) to three presentations of the same input (top panel). (b) Distribution of the correlation coefficient between pairs of responses of neuron 218 to repeated presentations of the same signal across trials (inter-series comparison, orange) and between pulses along time in the same trial (intra-series, blue). 10^5 pairs of responses were compared in each case.

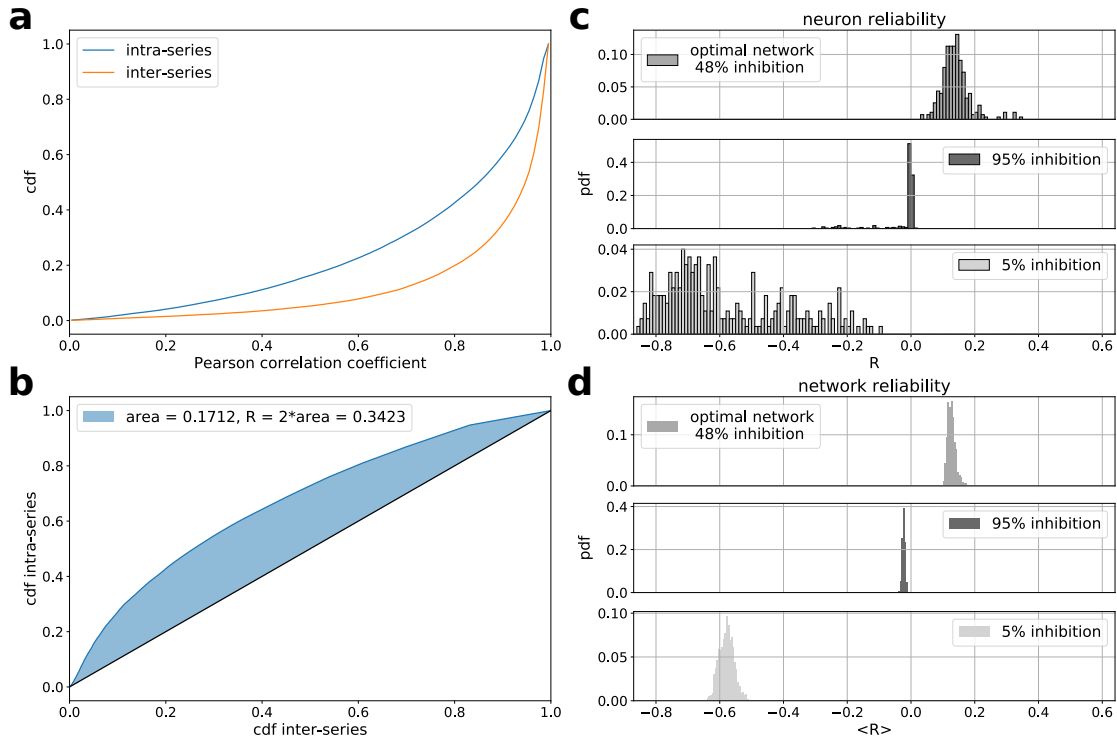


FIG. 6. Quantifying the reliable response of the *C. elegans* network. (a) Cumulative distribution function of the Pearson correlation coefficient between intra-series (blue) and inter-series (orange) pairs, for neuron 218 (Fig. 5b) in a network with 48% inhibition. (b) Corresponding receiver operating characteristic (ROC) curve of the two cumulative distribution functions, for the two distributions shown in panel a. (c) Distribution of the reliability coefficient for individual neurons, defined in terms of the blue area of panel b (see text). (d) Distribution of the reliability coefficient averaged over neurons for different network realizations.